

Each problem is worth 5 points. Clear and complete justification is required for full credit.

1. Evaluate $\int \frac{3}{(5y+1)^6} dy$.

$$\int \frac{3}{u^6} \cdot \frac{du}{5} = \frac{3}{5} \int u^{-6} du$$

$$= \frac{3}{5} \cdot -\frac{1}{5} u^{-5}$$

$$= -\frac{3}{5} \left(\frac{1}{5(5y+1)^5} \right) + C$$

Good

$$u = 5y + 1$$

$$\frac{du}{dy} = 5$$

$$dy = \frac{du}{5}$$

2. Evaluate $\int_0^{\pi} \sec^2(t/4) dt$.

$$4 \int_0^{\pi} \sec^2(u) du$$

$$4 \tan\left(\frac{1}{4}t\right) \Big|_0^{\pi}$$

$$4 \tan\left(\frac{1}{4}\pi\right) - 4 \tan\left(\frac{1}{4} \cdot 0\right)$$

$$4 - 0$$

$$\textcircled{4}$$

$$u = \frac{1}{4}t$$

$$\frac{du}{dt} = \frac{1}{4}$$

$$du \cdot 4 = dt$$

Wonderful!