

Each problem is worth 5 points. Clear and complete justification is required for full credit.

1. Parametrize and give bounds for the portion of the paraboloid $z = x^2 + y^2$ lying above the rectangle with vertices $(0,0)$, $(2,0)$, $(2,3)$, and $(0,3)$.

$$y(u,v) = v$$

$$x(u,v) = u$$

$$z(u,v) = u^2 + v^2$$

Wild!

$$0 \leq v \leq 3, \quad 0 \leq u \leq 2$$

2. Parametrize and give bounds for the portion of the cylinder with radius 3 centered around the x -axis between $x = 0$ and $x = 1$.

$$x(u,v) = u$$

$$y(u,v) = 3 \sin v$$

$$z(u,v) = 3 \cos v$$

Wacky!

$$0 \leq u \leq 1$$

$$0 \leq v \leq 2\pi$$

3. Parametrize and give bounds for a sphere with radius 2, centered at the origin.

$$z(u,v) = 2 \cos v$$

$$y(u,v) = 2 \sin v \sin u$$

$$x(u,v) = 2 \sin v \cos u$$

Zany!

$$0 \leq v \leq \pi$$

$$0 \leq u \leq 2\pi$$