

Quiz 1 Calculus 3 8/29/2012

Each problem is worth 5 points. Clear and complete justification is required for full credit.

1. Suppose $\mathbf{v} = \langle 8, -4 \rangle$ and $\mathbf{w} = \langle -4, 6 \rangle$. Express $3\mathbf{v} - \mathbf{w}$ in the form $\langle a, b \rangle$.

$$\begin{aligned}
 & 3\langle 8, -4 \rangle - \langle -4, 6 \rangle \\
 &= \langle 24, -12 \rangle + \langle +4, -6 \rangle \\
 &= \langle 28, -18 \rangle
 \end{aligned}$$

Good!

2. Consider the points $P(1,5,0)$ and $Q(0,7,2)$. Find two unit vectors parallel to \overrightarrow{PQ} , and write them in the form $ai + bj + ck$.

$$\begin{aligned}
 & \frac{\overrightarrow{PQ}}{|\overrightarrow{PQ}|} \quad \text{Nice} \\
 & \overrightarrow{PQ} = \langle (0-1), (7-5), (2-0) \rangle \\
 & \quad = \langle -1, 2, 2 \rangle \\
 & |\overrightarrow{PQ}| = \sqrt{(-1)^2 + 2^2 + 2^2} \\
 & \quad = \sqrt{9} \\
 & \quad = 3
 \end{aligned}$$

$$\begin{aligned}
 & \frac{-1}{3}, \frac{2}{3}, \frac{2}{3} \\
 & \underline{\underline{-\frac{1}{3}\hat{i} + \frac{2}{3}\hat{j} + \frac{2}{3}\hat{k}}} \\
 & \underline{\underline{\frac{1}{3}\hat{i} - \frac{2}{3}\hat{j} - \frac{2}{3}\hat{k}}}
 \end{aligned}$$