

1. Parametrize and give bounds for the portion of the paraboloid $z = x^2 + y^2$ lying above the rectangle with vertices $(0,0)$, $(2,0)$, $(2,3)$, and $(0,3)$.

$$x(u,v) = u$$

$$y(u,v) = v$$

$$z(u,v) = u^2 + v^2$$

$$\text{for } 0 \leq u \leq 2$$

$$0 \leq v \leq 3$$

2. Parametrize and give bounds for the portion of the cylinder with radius 4 centered around the z -axis between $z = 2$ and $z = 10$.

$$x(u,v) = 4 \cos u$$

$$y(u,v) = 4 \sin u$$

$$z(u,v) = v$$

$$\text{for } 0 \leq u \leq 2\pi$$

$$2 \leq v \leq 10$$

3. Parametrize and give bounds for the top half of a sphere with radius 5, centered at the origin.

$$x(u,v) = 5 \sin v \cos u$$

$$y(u,v) = 5 \sin v \sin u$$

$$z(u,v) = 5 \cos v$$

$$\text{for } 0 \leq u \leq 2\pi$$

$$0 \leq v \leq \pi/2$$