Each problem is worth 5 points. Keep your answers correct to the nearest thousandth.

1. If you use a left-hand sum with n = 3 subdivisions to approximate  $\int_4^7 \frac{1}{x} dx$ , what are:

$$\Delta x =$$

$$c_1 =$$

$$c_2$$
=

$$c_{3} =$$

$$f(c_1) =$$

$$f(c_2) =$$

$$f(c_3) =$$

$$f(c_3) = \sum_{i=1}^{3} f(c_i) \cdot \Delta x =$$

2. If you use a right-hand sum with n = 4 subdivisions to approximate  $\int_{5}^{9} x \, dx$ , what are:

$$\Delta x =$$

$$c_1 =$$

$$c_{2}^{-}$$

$$c_3 =$$

$$c_{4} =$$

$$f(c_1) =$$

$$f(c_2) =$$

$$f(c_3) =$$

$$f(c_4) =$$

$$\sum_{i=1}^{4} f(c_i) \cdot \Delta x =$$

3. If you use a midpoint sum with n = 4 subdivisions to approximate  $\int_1^3 \ln x \, dx$ , what are:

$$\Delta x =$$

$$c_1 =$$

$$c_{2}^{-}$$

$$c_3 =$$

$$c_4 =$$

$$f(c_1) =$$

$$f(c_2) =$$

$$f(c_3) =$$

$$f(c_4) =$$

$$c_{4} = f(c_{1}) = f(c_{2}) = f(c_{3}) = f(c_{4}) = \sum_{i=1}^{4} f(c_{i}) \cdot \Delta x = f(c_{4})$$

4. If you use a right-hand sum with *n* subdivisions to approximate  $\int_5^9 x \, dx$ , what are:

$$\Delta x =$$

$$c_k =$$

$$f(c_k) =$$

$$\sum_{k=1}^n f(c_k) \cdot \Delta x =$$

$$\lim_{n\to\infty}\sum_{k=1}^n f(c_k)\cdot\Delta x =$$