## Funsheet $2 \quad$ Calculus $1 \quad 10 / 20 / 22$

Each problem is worth 0 points... this time...

1. Show why the derivative of $\ln x$ is what it is.
(Research first if you need, but run your attempt by Jon for feedback!)
2. Let $f(x)=x \ln x-x$. Find $f^{\prime}(x)$ in the most simplified form you can manage.
3. Let $f(x)=\ln \left(x+\sqrt{9+x^{2}}\right)$. Find $f^{\prime}(x)$ in the most simplified form you can manage.
4. Let $f(x)=\ln (\sin x)$. Find $f^{\prime}(x)$ in the most simplified form you can manage.
5. Find a function of the form $f(x)=A b^{x}$ passing through the points $(1,20)$ and $(2,25)$.
6. (a) Find a function of the form $f(x)=A b^{x}$ passing through the points $(0,361)$ and $(10,439)$.
(b) Use your function from part (a) to find $\mathrm{f}(20)$. Compare your result with the data in \#6 of §3.4.
7. [Stewart] A sample of tritium-3 decayed to $94.5 \%$ of its original amount after a year.
(a) What is the half-life of tritium-3?
(b) How long would it take the sample to decay to $20 \%$ of its original amount?
8. [Stewart] A freshly brewed cup of coffee has temperature $95^{\circ} \mathrm{C}$ in a $20^{\circ} \mathrm{C}$ room. When its temperature is $70^{\circ} \mathrm{C}$, it is cooling at a rate of $1^{\circ} \mathrm{C}$ per minute. When does this occur?
