

Each problem is worth 5 points. For full credit provide complete justification for your answers.

1. Determine whether  $y = e^{3x}$  is a solution to the differential equation  $y'' - 4y' + 3y = 0$ .

$$y = e^{3x}$$

$$9e^{3x} - 4(3e^{3x}) + 3(e^{3x}) = 0$$

$$y' = 3e^{3x}$$

$$9e^{3x} - 12e^{3x} + 3e^{3x} = 0$$

$$y'' = 9e^{3x}$$

$$12e^{3x} - 12e^{3x} = 0$$

Yes, the

$$0 = 0$$

Solution works!! 😊

2. Determine whether  $y = x \sin x$  is a solution to the differential equation  $y'' + y = 2 \cos x$ .

$$y = x \sin x$$

$$2 \cos x - \cancel{x \sin x} + \cancel{x \sin x} = 2 \cos x$$

$$y' = \sin x + x \cos x$$

$$2 \cos x = 2 \cos x$$

$$y'' = \cos x + \cos x - x \sin x$$

$$y'' = 2 \cos x - x \sin x$$



Yes, solution works