Each problem is worth 5 points. For full credit provide proper justification for your answer.

1. Find the value of \( \int_{0}^{\infty} \frac{x}{e^x} \, dx \) or show that it diverges.

2. Find the area of the region bounded between \( y = x \) and \( y = 4x - x^2 \).