

Each problem is worth 5 points. Clear and complete justification is required for full credit.

1. Evaluate  $\int \frac{(\ln x)^3}{x} dx$ .

$$= \int \frac{u^3}{x} x du$$

$$= \int u^3 du = \frac{1}{4} u^4 + C$$

$$= \frac{1}{4} (\ln x)^4 + C$$

let  $\ln x = u$

$$\rightarrow \frac{du}{dx} = \frac{1}{x} \rightarrow dx = x du$$

Great

2. Evaluate  $\int \frac{x}{\sqrt[4]{x+2}} dx$ .

$$\int \frac{x}{u^{1/4}} du$$

$$\int \frac{u-2}{u^{1/4}} du$$

$$\int (u-2)(u^{-1/4}) du$$

$$\int (-2u^{-1/4} + u^{3/4}) du$$

$$- \frac{8}{3} u^{3/4} + \frac{4}{7} u^{7/4} + C$$

$$\left| -\frac{8}{3}(x+2)^{3/4} + \frac{4}{7}(x+2)^{7/4} + C \right|$$

let  $u = x+2$

$$\frac{du}{dx} = 1$$

$$dx = du$$

Using:

$$u = x+2$$

Solve for  $x$

$$\underline{u-2 = x}$$

Excellent!