

**Problem Set 4      Foundations      Due 2/23/2009**

Four of these problems will be graded, with each problem worth 5 points. Clear and complete justification is required for full credit. You are welcome to discuss these problems with anyone and everyone, but must write up your own final submission without reference to any sources other than the textbook and instructor. Submissions must be on clean paper with no ragged edges.

1. Give a careful algebraic proof that for any sets  $A$  and  $B$ ,  $B - (B - A) = A \cap B$ .
2. Let  $a, b \in \mathbb{R}$ . Show that  $a < b \Leftrightarrow a^2 < b^2$ .
3. Let  $a, b \in \mathbb{R}$ . Show that  $|a| + |b| \geq |a - b|$ .
4. Let  $x, y, z \in \mathbb{R}$ . Show that  $|x - y| \leq |x - z| + |z - y|$ .
5. Solve the inequality  $\frac{2x - 6}{x + 4} < 5$ .
6. Prove Theorem 3.4.3.