

You are encouraged to work in groups of two to four on this assignment and make a single group submission. Each problem is worth 3 points for correct and clearly justified answers. An additional quality point will be awarded to submissions which are presented in a manner appropriate to good college-level work.

1. Show that the value of the expression  $\int_0^x \frac{1}{1+t^2} dt + \int_0^{1/x} \frac{1}{1+t^2} dt$  does not depend on  $x$ .
2. Derive the integration formula  $\int \frac{x}{\sqrt{ax+b}} dx = \frac{2}{3a^2}(ax-2b)\sqrt{ax+b} + C$  [Line 83 on the table in the back of the book].
3. Consider the parabola  $y = x^2$ . Pick a point  $(a, a^2)$  on this parabola, and label it  $P$ . Label the point  $(-a, a^2)$  as  $Q$ . Find the lines tangent to the parabola at  $P$  and  $Q$ , and label their point of intersection  $R$ . Find the area of the region below segment  $PQ$  and above the parabola, and show that this area is equal to two-thirds of the area of triangle  $PQR$ .



You are encouraged to work in groups of two to four on this assignment and make a single group submission. Each problem is worth 3 points for correct and clearly justified answers. An additional quality point will be awarded to submissions which are presented in a manner appropriate to good college-level work.

1. Show that the value of the expression  $\int_0^x \frac{1}{1+t^2} dt + \int_0^{1/x} \frac{1}{1+t^2} dt$  does not depend on  $x$ .
2. Derive the integration formula  $\int \frac{x}{\sqrt{ax+b}} dx = \frac{2}{3a^2}(ax-2b)\sqrt{ax+b} + C$  [Line 83 on the table in the back of the book].
3. Consider the parabola  $y = x^2$ . Pick a point  $(a, a^2)$  on this parabola, and label it  $P$ . Label the point  $(-a, a^2)$  as  $Q$ . Find the lines tangent to the parabola at  $P$  and  $Q$ , and label their point of intersection  $R$ . Find the area of the region below segment  $PQ$  and above the parabola, and show that this area is equal to two-thirds of the area of triangle  $PQR$ .



You are encouraged to work in groups of two to four on this assignment and make a single group submission. Each problem is worth 3 points for correct and clearly justified answers. An additional quality point will be awarded to submissions which are presented in a manner appropriate to good college-level work.

1. Show that the value of the expression  $\int_0^x \frac{1}{1+t^2} dt + \int_0^{1/x} \frac{1}{1+t^2} dt$  does not depend on  $x$ .
2. Derive the integration formula  $\int \frac{x}{\sqrt{ax+b}} dx = \frac{2}{3a^2}(ax-2b)\sqrt{ax+b} + C$  [Line 83 on the table in the back of the book].
3. Consider the parabola  $y = x^2$ . Pick a point  $(a, a^2)$  on this parabola, and label it  $P$ . Label the point  $(-a, a^2)$  as  $Q$ . Find the lines tangent to the parabola at  $P$  and  $Q$ , and label their point of intersection  $R$ . Find the area of the region below segment  $PQ$  and above the parabola, and show that this area is equal to two-thirds of the area of triangle  $PQR$ .



You are encouraged to work in groups of two to four on this assignment and make a single group submission. Each problem is worth 3 points for correct and clearly justified answers. An additional quality point will be awarded to submissions which are presented in a manner appropriate to good college-level work.

1. Show that the value of the expression  $\int_0^x \frac{1}{1+t^2} dt + \int_0^{1/x} \frac{1}{1+t^2} dt$  does not depend on  $x$ .
2. Derive the integration formula  $\int \frac{x}{\sqrt{ax+b}} dx = \frac{2}{3a^2}(ax-2b)\sqrt{ax+b} + C$  [Line 83 on the table in the back of the book].
3. Consider the parabola  $y = x^2$ . Pick a point  $(a, a^2)$  on this parabola, and label it  $P$ . Label the point  $(-a, a^2)$  as  $Q$ . Find the lines tangent to the parabola at  $P$  and  $Q$ , and label their point of intersection  $R$ . Find the area of the region below segment  $PQ$  and above the parabola, and show that this area is equal to two-thirds of the area of triangle  $PQR$ .



You are encouraged to work in groups of two to four on this assignment and make a single group submission. Each problem is worth 3 points for correct and clearly justified answers. An additional quality point will be awarded to submissions which are presented in a manner appropriate to good college-level work.

1. Show that the value of the expression  $\int_0^x \frac{1}{1+t^2} dt + \int_0^{1/x} \frac{1}{1+t^2} dt$  does not depend on  $x$ .
2. Derive the integration formula  $\int \frac{x}{\sqrt{ax+b}} dx = \frac{2}{3a^2}(ax-2b)\sqrt{ax+b} + C$  [Line 83 on the table in the back of the book].
3. Consider the parabola  $y = x^2$ . Pick a point  $(a, a^2)$  on this parabola, and label it  $P$ . Label the point  $(-a, a^2)$  as  $Q$ . Find the lines tangent to the parabola at  $P$  and  $Q$ , and label their point of intersection  $R$ . Find the area of the region below segment  $PQ$  and above the parabola, and show that this area is equal to two-thirds of the area of triangle  $PQR$ .

