You are expected to do the following problems to a high standard (i.e., at least well enough to be published in a textbook) for full credit. Five of these problems will be selected (by Jon) for grading, with each worth 4 points.

- 1. [Baker Ch 2 R1] The empty set is a closed subset of  $\mathbb{R}$  regardless of the topology on  $\mathbb{R}$ .
- 2. [Baker Ch 2 R2] Any open interval is an open subset of  $\mathbb{R}$  regardless of the topology on  $\mathbb{R}$ .
- 3. [Baker Ch 2 R3] Any closed interval is a closed subset of  $\mathbb{R}$  regardless of the topology on  $\mathbb{R}$ .
- 4. [Baker Ch 2 R4] A half-open interval of the form [a, b) is neither an open set nor a closed set regardless of the topology on  $\mathbb{R}$ .
- 5. [Baker Ch 2 R5] If A is a subset of a topological space, then  $A \subseteq Cl(A)$ .
- 6. [Baker Ch 2 R6] If A is a subset of a topological space, then  $A' \subseteq A$ .
- 7. [Baker Ch 2 R7] For any closed subset A of a topologoical space,  $A' \subseteq A$ .
- 8. [Baker Ch 2 R8] If A is a subset of a topological space, then  $Int(A) \subseteq A$ .
- 9. [Baker Ch 2 R9] For any subset *A* of a topological space,  $Bd(A) \subseteq A$ .
- 10. [Baker Ch 2 R10] If *A* is a subset of a topological space, then  $Bd(A) \subseteq Cl(A)$ .
- 11. [Baker Ch 2 R11] If A is a closed subset of a topological space, then  $Bd(A) \subseteq A$ .
- 12. [Baker Ch 2 R12] If *A* is a subset of a topological space, then  $Int(A) \subseteq Cl(A)$ .
- 13. [Baker Ch 2 R13] The point 1 is a limit point of the set [0, 1) regardless of the topology on  $\mathbb{R}$ .

- 14. [Baker Ch 2 R14] The point 2 is not a limit point of the set [0,1) regardless of the topology on  $\mathbb{R}$ .
- 15. [Baker Ch 2 R15] For any subset A of a topological space, Ext(A) = X A.
- 16. [Baker Ch 2 R16] For any closed subset A of a topological space, Ext(A) = X A.
- 17. [Baker Ch 2 R17] The collection  $\mathcal{B} = \{\{x\} : x \in \mathbb{R}\}$  is a base for a topology on  $\mathbb{R}$ .
- 18. [Baker Ch 2 R18] The collection  $\mathcal{B} = \{\{x\} : x \in \mathbb{R}\}$  is a base for the usual topology on  $\mathbb{R}$ .
- 19. [Baker Ch 2 R19] In a space  $(X, \mathcal{T})$  any collection of open sets whose union equals X and that is closed under finite intersection is a base for  $\mathcal{T}$ .
- 20. [Baker Ch 2 R20] There exists a topological space  $(X, \mathcal{T})$  such that there is no base for  $\mathcal{T}$ .
- 21. [Baker Ch 2 R21] There exists a topological space  $(X, \mathcal{T})$  for which there is more than one base for  $\mathcal{T}$ .