Each problem is worth 10 points. For full credit provide good justification for your answers.

1. Set up an integral for the area of the region bounded between $y=x^2$ and y=2x.

2. Set up an integral for the volume of the solid obtained when the region from #1 is rotated around the x-axis.

3. If the work required to stretch a spring 1 ft beyond its natural length is 12 ft-lb, how much work (in ft-lb) is needed to stretch it 9 in. beyond its natural length?

4. Set up an integral for the length of the portion of the curve y = x(3-x) that lies above the x-axis.

5. A bank account earns 6 percent interest compounded continuously. At what (constant, continuous) rate must a parent deposit money into such an account in order to save 100000 dollars in 18 years for a child's college expenses?

6. Find the x-coordinate of the center of mass of the region lying underneath the graph of the function $f(x) = \sqrt{x}$ over the interval [0, 25].

7. Star is a calculus student at Enormous State University, and they're having some trouble. Star says "Geez! Calc 2 is so different from Calc 1! It used to be there was, like, just one right way to do things, right? But now I did this area as $\int_0^1 (x-x^2) dx$ but the professor was saying you could do it $\int_0^1 (\sqrt{y}-y) dy$. Is it just a coincidence that they both work, or what?"

Help Star out. Explain to them as clearly as possible why both ways work for the same region.

8. A gas station stores its gasoline in a tank under the ground. The tank is a cylinder lying horizontally on its side. (In other words, the tank is not standing vertically on one of its flat ends.) If the radius of the cylinder is 1 meter, its length is 5 meters, and its top is 3 meters under the ground, set up an integral for the total amount of work needed to pump the gasoline out of the tank to ground level. (The density of gasoline is 673 kilograms per cubic meter; use $g = 9.8m/s^2$).

9. Consider the entire region bounded between $y=x^3$ and y=2x. If this region is revolved around the axis x=3, set up an integral or integrals for the volume of the resulting solid.



Extra Credit [5 points possible]: [Ellis & Gullick] Assume that [a,b] is a closed interval contained in the open interval (-1,1). Let $f(x) = \sqrt{1-x^2}$ and let S be the surface area of the region obtained by revolving the graph of f on [a,b] about the x axis. Show that

$$S = 2\pi(b - a)$$