## Exam 3b $\quad$ Foundations of Advanced Math 3/22/24

1. Let $f, g: \mathbb{R} \rightarrow \mathbb{R}$, and suppose that $f$ and $g$ are both odd functions. Then $f+g$ is an (even / odd - pick one and defend your claim) function.
2. If $f: A \rightarrow B$ and $g: B \rightarrow C$ are injective functions, then $g \circ f$ is injective.
3. If $f, g: \mathbb{R} \rightarrow \mathbb{R}$ are both bounded, then:
(a) $f+g$ is bounded
(b) $f / g$ is bounded
4. If $A, B$ and $C$ are denumerable sets with each pair disjoint, then $A \cup B \cup C$ is denumerable.
5. (a) The set of even natural numbers is denumerable.
(b) The set of irrational numbers is uncountable.
