

Each problem is worth 5 points. For full credit indicate clearly how you reached your answer.

1. Find $\lim_{(x,y) \rightarrow (0,0)} \frac{(x+y)^2}{x^2+y^2}$, or show that it does not exist.

$x=0$

$$\lim_{(0,y)} \frac{(0+y)^2}{0+y^2} = \frac{y^2}{y^2} = 1$$

$y=x$

$$\lim_{y=x} \frac{(x+x)^2}{x^2+x^2} = \frac{(2x)^2}{2x^2} = \frac{4x^2}{2x^2} = 2 \quad \text{Great}$$

$1 \neq 2$, so the limit does not exist.

2. If $f(x,y) = xy^2 - e^x + \cos(xy)$, find f_x and f_y .

5/5

$$f_x(x,y) = y^2 - e^x + (-\sin(xy)y) \quad \{ \text{Assume all } y \text{ are constants} \}$$

$$f_y(x,y) = 2xy - 0 + (-\sin(xy)x) \quad \{ \text{Assume all } x \text{ are constants} \}$$

e^x is a number in original because x is constant. Deriv. of constant is 0

Great

3. State the definition of the derivative of a function $f(x,y)$ with respect to x .

5/5

$$f_x(x,y) = \lim_{h \rightarrow 0} \frac{f(x+h, y) - f(x, y)}{h}$$

