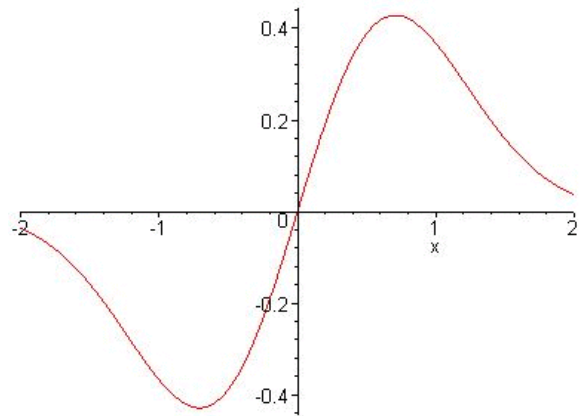
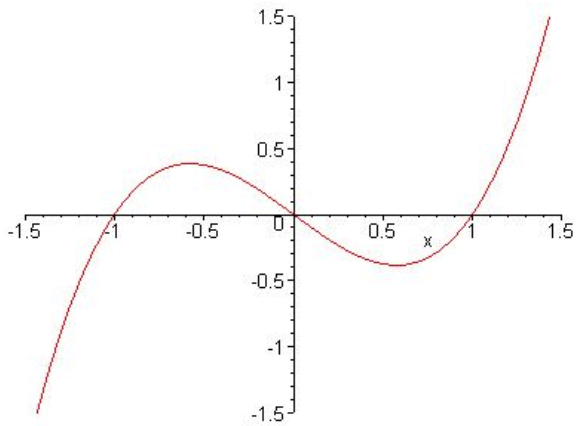


Exam 1 Calculus 1 9/20/2002

Each problem is worth 10 points. Show adequate justification for full credit. Please circle all answers and keep your work as legible as possible. Past returns do not assure future performance.

1. State the definition of the derivative $f'(x)$ of a function $f(x)$.

2. Two graphs are shown below. For each graph, sketch a graph of the derivative of the function shown on the same set of axes.



Use the graph of $f(x)$ shown at right for problems 3 and 4:

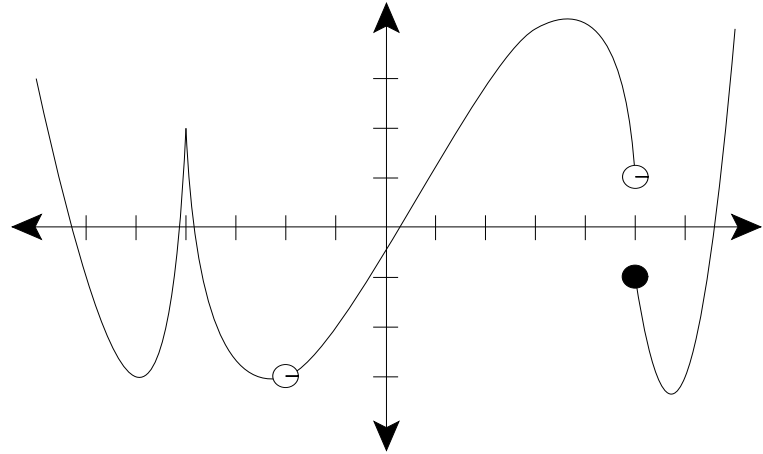
3. (a) What is $\lim_{x \rightarrow 3^-} f(x)$?

(b) What is $\lim_{x \rightarrow 3^+} f(x)$?

(c) What is $\lim_{x \rightarrow 3} f(x)$?

(d) What is $f(5)$?

(e) What is $f(-2)$?



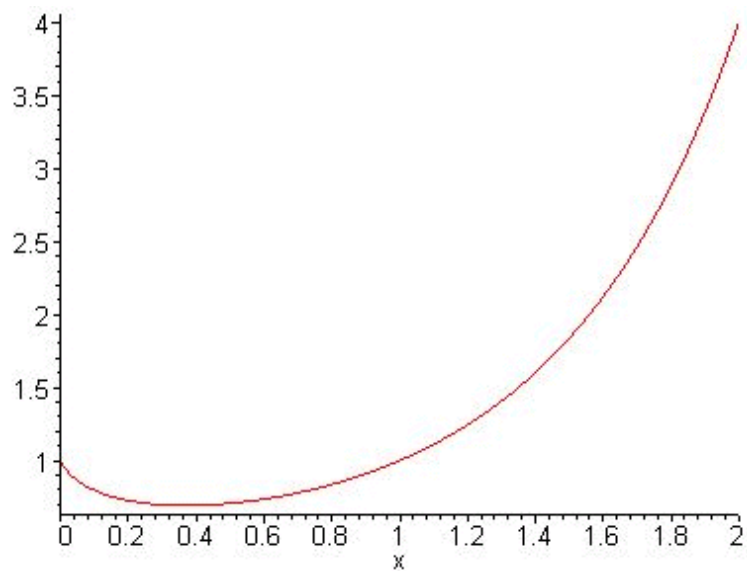
4. (a) For what values of x is $f(x)$ discontinuous?

(b) For what values of x is $f(x)$ not differentiable?

5. Let $f(x) = x^3 - 5x$. If you know that $f'(x) = 3x^2 - 5$, write an equation for the line tangent to $f(x)$ when $x=1$.

6. Compute $\lim_{x \rightarrow \infty} \left(\sqrt{x^2 + 1} - \sqrt{x^2 - 1} \right)$.

7. A graph of $f(x) = x^x$ is shown below. Estimate the value of $f'(1.5)$ accurate to at least the nearest hundredth.



8. Show that if $f(x) = \frac{1}{x}$, then $f'(x) = \frac{-1}{x^2}$.

9. The land that Jon and Darcy's house is built on was appraised at \$15,550 in 2001 and \$32,480 in 2002. Darcy says "So the value went up by \$16,930 in just a year. If it keeps going like that, it'll be \$49,410 next year." Jon answers "No, it's even better than that, since it more than doubled in just a year, if it keeps going like that it'll be \$67,842 next year."

Explain clearly to Jon and Darcy what they should expect for their 2003 appraisal. [Yes, this is a vague question – but you've got the tools to give really good answers, so see what you can do.]

10. Samantha is a calculus student at Enormous State University, and she's having some trouble with limits. Samantha says "So, like, I totally bombed this quiz we had about limits. We were supposed to say what the limit of things like $\frac{n-1}{n}$ was, and so I said I didn't really know, but for sure it had to be less than 1, because stuff like $\frac{1}{2}$ and $\frac{2}{3}$ and all that are less than 1. So whatever the limit is, it's gotta be less than 1 too, right? But the professor didn't really like it, I guess, and he wrote this long note I totally couldn't even read, and I got no points, so I really better figure this out for the exam, huh?"

Help Samantha by explaining, in terms she can understand, either how to convince her professor she's right, or how it is that terms less than 1 can have a limit equal to 1.

Extra Credit (5 points possible):

If $f(x) = \sqrt[3]{x}$, use the definition of the derivative to find $f'(x)$. Partial credit just for setting it up.