

4. Find the Jacobian for the transformation $x = u + 4v$, $y = 3u - 2v$.

5. **Set up** an iterated integral for the **surface area** of the part of the cylinder $y^2 + z^2 = 9$ that lies above the rectangle with vertices $(0,0)$, $(4,0)$, $(0,2)$, and $(4,2)$.

6. **Set up** iterated integrals for the **center of mass** of a triangular lamina of density $\rho(x,y) = k$ with vertices $(0,0)$, $(a,0)$, and $(0,b)$.

7. If $[x]$ denotes the greatest integer less than or equal to x , **evaluate** the integral $\iint_R \left[\sqrt{x^2 + y^2} \right] dA$ where R is the disk with center at the origin and radius 3.

8. Muffy is a calculus student at E.S.U., and she's having trouble with multiple integrals. Muffy says "Ohmygod, I so totally failed my Calc exam. There were totally impossible problems on it, and I think it's totally bad, and my daddy is going to sue the school. There was this one that was like, you were supposed to find the region-thingy for this integral $\iiint_D (1 - x^2 - y^2 - z^2) dV$ to

be the biggest it could be, and I said, like, obviously it's bigger if you do it for a bigger region-thingy, right? So, it must be biggest if you have D be like all of \mathbb{R}^3 , right? But I got no points, so Daddy's going to get the professor fired.

Clarify for Muffy, in terms she can understand, how she should think about a problem like this, and what region D in fact maximizes the given integral.

9. Find the exact value of $\int_0^4 \int_0^1 \int_{2y}^2 \frac{2 \cos(x^2)}{\sqrt{z}} dx dy dz$.

10. Pat the mathematician has gone completely off the deep end and is now leaving the mainstream catering business for the highly specialized sausage sculpture niche business. Pat is trying to figure out the volume of novel sausage sections. Suppose the sausage is shaped like the cylinder $x^2+y^2=1$, with one cut made perpendicular to the cylinder along the plane $z=0$ and the other cut made along a paraboloid shaped like $z = x^2 + y^2$ but translated to have its vertex at $(a,b,0)$. **Set up** an iterated integral for the resulting volume and **evaluate** it.

Extra Credit (up to 5 points possible):

Show that if $L(x,y)$ is a plane, then the average value of $L(x,y)$ over the region $R = \{(x,y) | 0 \leq x \leq 400, 0 \leq y \leq 200\}$ is equal to the average of $L(400,0)$ and $L(0,200)$.