Fake Quiz 2Real Analysis 111/18/2002

Each problem is worth 0 points, this time at least.

- 1. State the definition of the limit of a function $f: \mathbb{R} \to \mathbb{R}$ at a point a.
- 2. State the definition of the limit of a function $f: \mathbb{R} \to \mathbb{R}$ as x approaches infinity.
- 3. State the definition of continuity of a function $f: \mathbb{R} \to \mathbb{R}$ at a point a.
- 4. State the definition of the derivative of a function $f: \mathbb{R} \rightarrow \mathbb{R}$ at a point a.
- 5. State the Intermediate Value Theorem.
- 6. State Rolle's Theorem.
- 7. State the Mean Value Theorem.

8. Prove that
$$\lim_{x\to\infty}\frac{1}{x^2}$$
 exists.

9. Give an example of a function $f:[0,1] \rightarrow \mathbb{R}$ which is discontinuous at every point but for which |f(x)| is differentiable at every point.

10. Prove that if $f:\mathbb{R}\to\mathbb{R}$ and $g:\mathbb{R}\to\mathbb{R}$ are both continuous functions, then (f+g) is also continuous.

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