

Fake Quiz 4    Real Analysis 1    11/22/2002

Each problem is worth 0 points, this time at least.

1. What does it mean for a function to be continuous on a set  $E$ , as opposed to just continuous at a point  $a$ ?
2. Give an example of a function  $f: \mathbb{R} \rightarrow \mathbb{R}$  for which the limit as  $x$  approaches 3 does not exist.
3. Give an example of a function for which  $\lim_{x \rightarrow \infty} f(x)$  is infinite, but  $\lim_{x \rightarrow \infty} f'(x)$  is finite.
4. State the Extreme Value Theorem.
5. Prove or give a counterexample: If  $f(3)=5$ , then  $f'(-3)=-5$ .
6. Prove or give a counterexample: If  $f(3)=5$  and  $f'(-3)=-5$ , then  $f$  is even.
7. Is it true that every function which is differentiable is twice differentiable?
8. Prove or give a counterexample: If  $I=[a,b]$  is an interval and  $f: I \rightarrow \mathbb{R}$  is an increasing function, then the point  $a$  is an absolute minimum for  $f$  on  $I$ .
9. Show that if  $f$  and  $g$  are increasing functions on an interval  $I \subseteq \mathbb{R}$ , then  $f+g$  is an increasing function on  $I$  as well.
10. Show that  $f(x) = \sqrt[3]{x}$  is not differentiable at  $x=0$ .