

Each problem is worth 5 points. For full credit indicate clearly how you reached your answer.

1. Find exact values for all solutions (in radians) to the equation $2\cos x + 1 = 0$.

$$2\cos x = -1$$

$$\cos x = -1/2$$

$$\cos^{-1}(\cos x) = \cos^{-1}(-1/2)$$

$$x = \cos^{-1}(-1/2)$$

$$x = \frac{2\pi}{3} + 2\pi n \text{ for any integer } n$$

$$\text{or } x = \frac{4\pi}{3} + 2\pi n \text{ for any integer } n$$

$$2\pi - \frac{2\pi}{3} = \frac{4\pi}{3}$$

2. Verify the trig identity $\cot^2 \theta - \cos^2 \theta = \cot^2 \theta \cos^2 \theta$.

I'll work with the left-hand side:

$$\cot^2 \theta - \cos^2 \theta =$$

$$\frac{\cos^2 \theta}{\sin^2 \theta} - \frac{\cos^2 \theta}{1} =$$

$$\frac{\cos^2 \theta - \cos^2 \theta \cdot \sin^2 \theta}{\sin^2 \theta} =$$

$$\frac{\cos^2 \theta (1 - \sin^2 \theta)}{\sin^2 \theta} =$$

$$\frac{\cos^2 \theta}{\sin^2 \theta} \cdot \frac{\cos^2 \theta}{1} =$$

$$\cot^2 \theta \cdot \cos^2 \theta = \cot^2 \theta \cdot \cos^2 \theta \quad \checkmark$$