Each problem is worth 5 points. For full credit indicate clearly how you reached your answer.

1. Do the parabolas $y=-1-x^{2}$ and $y=1+x^{2}$ have any tangent lines in common? Find equation(s) of any such lines, and explain why more cannot exist.
2. Suppose that on a surprisingly warm October day the high temperature of $87^{\circ}$ occurs at exactly 4 pm , with the low temperature of $49^{\circ}$ having occurred at exactly 4 am . Find a formula for a function that does a good job of representing the temperature throughout the day, and use it to find the rate at which the temperature is changing at 2 pm .
3. Find $\lim _{x \rightarrow 0^{+}} x \ln x$.
4. Find $\lim _{x \rightarrow \infty}\left(x-\sqrt{x^{2}-x}\right)$.
