

Each problem is worth 5 points. Clear and complete justification is required for full credit.

1. Find the most general antiderivative of the function $f(x) = \frac{10}{x^9}$.

$$f(x) = 10x^{-9}$$

$$\int 10x^{-9} dx = \frac{10x^{-8}}{-8} + C$$

$$-\frac{5}{4}x^{-8} + C$$

Well done

2. If $f''(x) = 2 - 12x$, $f(0) = 9$, and $f(2) = 15$, find $f(x)$.

$$f'(x) = 2x - 6x^2 + C$$

$$f(x) = x^2 - 2x^3 + Cx + D$$

$$f(0) = 0 - 0 + 0 + D = 9$$

$$D = 9$$

$$f(2) = 2^2 - 2(2)^3 + C(2) + 9 = 15$$

$$4 - 16 + 2C + 9 = 15$$

$$2C = 18$$

$$C = 9$$

$$f(x) = -2x^3 + x^2 + 9x + 9$$

Great