

Each problem is worth 5 points. Clear and complete justification is required for full credit.

1. Evaluate $\int \frac{(\ln x)^2}{x} dx$.

$$u = \ln x \quad du = \frac{1}{x} dx$$

$$dx = x du$$

$$= \int \frac{u^2}{x} x du$$

$$= \int u^2 du$$

$$= \frac{u^3}{3} + C$$

$$= \frac{(\ln x)^3}{3} + C$$

Excellent

2. Evaluate $\int \frac{1+x}{1+x^2} dx$

$$\int \frac{1}{1+x^2}$$

$$+ \int \frac{x}{1+x^2}$$

$$u = 1+x^2$$

$$du = 2x dx$$

$$\int \frac{x}{u} \cdot \frac{du}{2x}$$

$$dx = \frac{du}{2x}$$

$$\frac{1}{2} \int \frac{1}{u} du$$

$$\tan^{-1} x + \frac{1}{2} \ln |u| + C$$

Nice
Job!

always have the
positive sign
no abs. val.

$$\tan^{-1} x + \frac{1}{2} \ln(1+x^2) + C$$