

Several of these problems will be graded, with each graded problem worth 5 points. Clear, complete, and legible justification is required for full credit. You are welcome to discuss these problems with anyone and everyone, but must write up your own final submission without reference to any sources other than the textbook and instructor.

1. Give an example of a function, interval, and partition \mathcal{P} for which a left-hand sum using \mathcal{P} is closer to the actual value of the Riemann integral than the left-hand sum using a partition \mathcal{Q} which is a refinement of \mathcal{P} .
2. Evaluate $\int_0^3 x^2 dx$ using upper and lower sums as in Example 6.1.7.
3. Prove Lemma 6.1.3.
4. Prove that $U(\mathcal{Q}, f) \leq U(\mathcal{P}, f)$ in Lemma 6.1.5.
5. Prove Theorem 6.2.2 in the case where the function f is decreasing.
6. Do Problem 10(b) in §6.2.

