## Handout 1 Graph Theory 11/2/11

## Trees

A connected graph with no cycle is called a tree.

Problem 102 Find all trees (distinct up to isomorphism) with fewer than 7 vertices.
Problem 103 Find all trees with 7 vertices.

Problem 104 Find all trees with 8 vertices.

Problem $105 G$ is a tree if and only if every two vertices of $G$ are joined by a unique path.
Problem $106 G$ is a tree if and only if $G$ is connected and $p=q+1$.
Problem $107 G$ is a tree if and only if $G$ has no cycles and $p=q+1$.
Problem 108 Which trees are bipartite graphs?

Problem $109 G$ is a tree if and only if every edge of $G$ is a bridge.

