Four of these problems will be graded, with each problem worth 5 points. Clear and complete justification is required for full credit. You are welcome to discuss these problems with anyone and everyone, but must write up your own final submission without reference to any sources other than the textbook and instructor.

- 1. If a sequence $\{a_n\}$ converges to 0, and a sequence $\{b_n\}$ is bounded, then the sequence $\{a_nb_n\}$ converges to 0.
- 2. If a sequence $\{a_n\}$ converges to 0, and $\{a_nb_n\}$ converges to zero, then the sequence $\{b_n\}$ is bounded.
- 3. Determine whether $\lim_{n\to\infty}\frac{1}{n}\sin\frac{1}{n}$ exists, and find its value. [Kosmala 2.2.11(l)]
- 4. Consider the sequences $\{a_n\}$ and $\{b_n\}$, where sequence $\{a_n\}$ converges to zero. Then $\{a_nb_n\}$ converges to zero. [Kosmala 2.2.12]
- 5. If a sequence $\{a_n\}$ diverges to $+\infty$ and $a_n \le b_n$ for all $n \ge n_1$, then the sequence $\{b_n\}$ must also diverge to $+\infty$.
- 6. Do Exercise 2.3.4.
- 7. If sequences $\{a_n\}$ and $\{b_n\}$ diverge to $+\infty$, then $\{a_nb_n\}$ diverges to $+\infty$. [Kosmala 2.3.5]
- 8. Suppose that the sequence $\{a_n\}$ diverges to $+\infty$. Find examples of sequences $\{a_n\}$ and $\{b_n\}$ so that $\{\frac{a_n}{b_n}\}$
 - (a) diverges to $+\infty$.
 - (b) converges to 7.
 - (c) converges to 0.
 - (d) diverges to $-\infty$.
 - (e) oscillates.