

Quiz 1 Calculus 3 10/26/21

Each problem is worth 5 points. Clear and complete justification is required for full credit

1. Give parametric equations $x(t)$, $y(t)$, $z(t)$ and bounds for t that produce a path from $(1, 5, 1)$ to $(4, 3, 2)$.

$$\begin{aligned} x(t) &= 1 + 3t \\ y(t) &= 5 + (-2t) \\ z(t) &= 1 + t \end{aligned}$$

$$0 \leq t \leq 1$$

Good

Check:

$$x(0) = 1 \quad \checkmark$$

$$y(0) = 5 \quad \checkmark$$

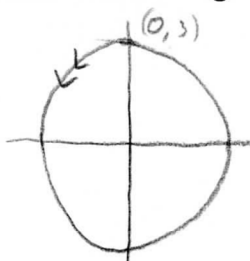
$$z(0) = 1 \quad \checkmark$$

$$x(1) = 4 \quad \checkmark$$

$$y(1) = 3 \quad \checkmark$$

$$z(1) = 2 \quad \checkmark$$

2. Give parametric equations $x(t)$ and $y(t)$ and bounds for t that produce a circle with radius 3 centered at the origin traversed 2 complete times beginning and ending at $(0, 3)$.



$$\begin{aligned} x(t) &= 3 \cos(t) \\ y(t) &= 3 \sin(t) \end{aligned} \quad \frac{\pi}{2} \leq t \leq \frac{9\pi}{2}$$

We start with $t = \frac{\pi}{2}$ so the starting point is $(0, 3)$. Since we are asked to traverse it twice, going to $\frac{5\pi}{2}$ is not enough, we need to travel it again up to $\frac{9\pi}{2}$

Nice!