

Each problem is worth 5 points. Keep your answers correct to the nearest thousandth.

1. If you use a left-hand sum with $n = 3$ equal subdivisions to approximate $\int_1^4 \frac{1}{x} dx$, what are:

$$\Delta x =$$

$$c_1 =$$

$$c_2 =$$

$$c_3 =$$

$$f(c_1) =$$

$$f(c_2) =$$

$$f(c_3) =$$

$$\sum_{i=1}^3 f(c_i) \cdot \Delta x =$$

2. If you use a right-hand sum with $n = 3$ equal subdivisions to approximate $\int_1^4 \frac{1}{x} dx$, what are:

$$\Delta x =$$

$$c_1 =$$

$$c_2 =$$

$$c_3 =$$

$$f(c_1) =$$

$$f(c_2) =$$

$$f(c_3) =$$

$$\sum_{i=1}^3 f(c_i) \cdot \Delta x =$$

3. If you use a midpoint sum with $n = 4$ equal subdivisions to approximate $\int_1^3 \ln x \, dx$, what are:

$$\Delta x =$$

$$c_1 =$$

$$c_2 =$$

$$c_3 =$$

$$c_4 =$$

$$f(c_1) =$$

$$f(c_2) =$$

$$f(c_3) =$$

$$f(c_4) =$$

$$\sum_{i=1}^4 f(c_i) \cdot \Delta x =$$

4. If you use a midpoint sum with $n = 5$ equal subdivisions to approximate $\int_0^1 \sin(x^2) \, dx$, what are:

$$\Delta x =$$

$$c_1 =$$

$$c_2 =$$

$$c_3 =$$

$$c_4 =$$

$$c_5 =$$

$$f(c_1) =$$

$$f(c_2) =$$

$$f(c_3) =$$

$$f(c_4) =$$

$$f(c_5) =$$

$$\sum_{i=1}^5 f(c_i) \cdot \Delta x =$$