

Each problem is worth 5 points. For full credit provide proper justification for your answer.

1. Determine whether $y = 2\cos 4x$ is a solution to the differential equation $\frac{d^2y}{dx^2} = -4y$.

$$y = 2 \cos 4x$$

$$y' = -8 \sin 4x$$

$$\underline{y'' = -32 \cos 4x}$$

$$-4(2 \cos 4x) \stackrel{?}{=} -32 \cos 4x$$

$$\underline{-8 \cos 4x} \neq \underline{-32 \cos 4x}$$

Good

NO

2. Determine whether the function $y = xe^{-3x}$ is a solution to the differential equation $3y + y' = y/x$.

$$3y + y' = \frac{y}{x}$$

$$3(\underline{xe^{-3x}}) + (\underline{xe^{-3x}})' = \frac{\cancel{x}e^{-3x}}{\cancel{x}}$$

Nice
Job

$$\cancel{3x}e^{-3x} + e^{-3x} + x(-3)e^{-3x} = e^{-3x}$$

$$e^{-3x} = e^{-3x}$$

Yes,

function is a solution