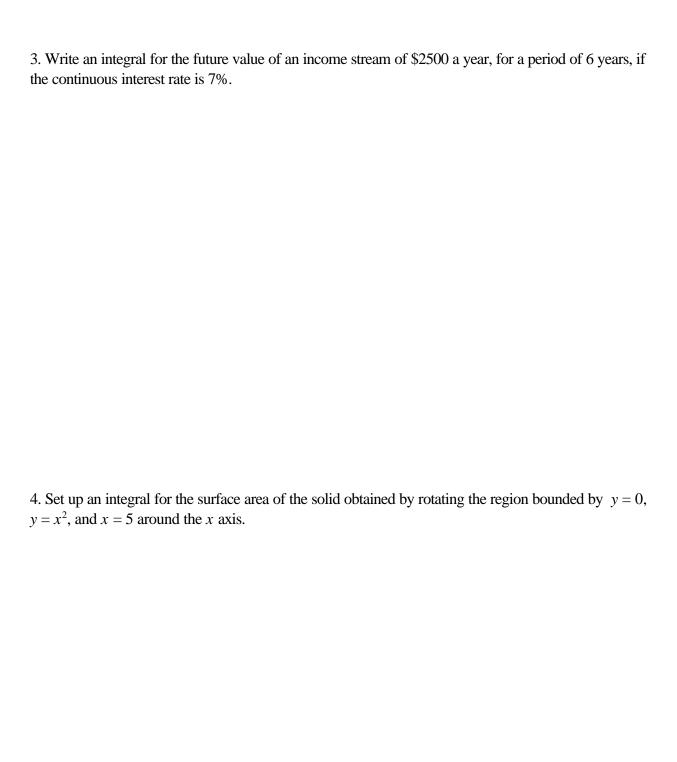
## Exam 2b Calc 2 2/25/2005

Each problem is worth 10 points. For full credit provide complete justification for your answers.

1. Set up an integral for the area of the portion of the circle  $x^2 + y^2 = 25$  which lies to the right of the line x = 1.

2. Set up an integral for the arc length of the portion of the curve  $y = x^3$  between the points (-1,-1) and (2,8).



5. Write an integral or integrals for portion of a circle with radius 5.	$\overline{x}$ , the x coordinate of the center of mass of the first-quadrant

6. If a spring requires 10 foot-pounds of work to stretch it from a natural length of 24 inches to 30 inches, to what total length (to the nearest tenth of an inch) will 20 foot-pounds of work stretch it?	

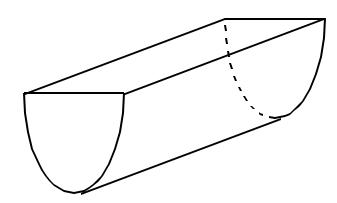
7. Bunny is a calculus student at Anonymous State University, and she's having some trouble with antiderivatives. Bunny says "Ohmygod, calculus has gotten *so* hard. There's this probability stuff, you know? And like, it's so confusing? My notes are a total mess, and I don't know what they mean at all. It's something like, maybe, like, if you integrate it from zero to one, then it's supposed to be infinite, I think. But I don't know what that means!"

Explain clearly to Bunny a couple of key things to know about probability density functions, including at least one thing involving the "zero to one" interval she mentions, and at least one thing involving infinity.

8. If 
$$p(x) = \begin{cases} 0.3e^{-0.3x} & \text{if } x \ge 0 \\ 0 & \text{if } x < 0 \end{cases}$$
 is a probability density function giving the probability of a baby

rhinoceros taking its first steps x days after birth, compute the mean number of days after birth for a rhinoceros to take its first steps.

9. Jon is planning to go into business selling new underground gasoline storage tanks to gas stations. The tanks will be shaped like the picture shown below, where the front and back faces are shaped like the parabola  $y = x^2$  between (-2,4) and (2,4), and from front to back the tank measures 10 feet. Jon intends to market these tanks based on the claim that since more of the tank is near the surface than in a standard storage tank shaped like a cylinder lying on its side, the amount of work the pumps need to do will be less with these tanks than with conventional tanks. Set up an integral for the amount of work required to pump all the gasoline in one of Jon's tanks to a point 6 feet above the top of the tank (gasoline weighs 42 lb/ft<sup>3</sup>).



10. Suppose that f(x) is a function, (with  $f(x) \ge 0$  everywhere) the area beneath which (but above the x axis) from x = a to x = b is given by A, and that the volume of the solid obtained by rotating the region beneath f(x) around the x axis is given by V. Let g(x) be another function, with g(x) = f(x) + 2. Express the volume of the solid obtained by rotating the region below g(x) between x = a and x = b in terms of the values A and V.

Extra Credit (5 points possible):

The solid obtained by revolving the region beneath the curve with equation  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  around the x axis is called a hyperboloid of one sheet. Compute the volume of the portion of a hyperboloid of one sheet which lies between x = a and x = c.