Examlet 3b Foundations of Advanced Math 3/23/07

1. a) State the definition of an increasing function

b) Give an example of a set which is not countable.

2. Is the product of an even function with an odd function even or odd? Support your answer.

3. Let $f: A \to B$ and $g: B \to C$ both be injections. Show that $g \circ f$ is injective.

4. Suppose that *A* is a denumerable set, and let $B = \{1,2,3\}$. Prove that $A \times B$ is denumerable, or prove that it isn't.

5. Show that for any $a, b \in \mathbb{R}$ with a < b, (a, b) and \mathbb{R} are equipollent.