# Special Topics: Game Theory 1:00pm MWF Spring 2009 SH309 

| Instructor: | Jonathan White |
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| Office Hours: | $11: 00-11: 25$ MWF, 3:00-3:25 MW, and by appointment |
| Office Phone: | $399-8280$ |
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| Text: | Lessons in Play: An Introduction to Combinatorial Game Theory, by Albert, Nowakowski, <br> and Wolfe |

This course will work very differently, both in terms of daily conduct and grading, than typical math courses. My hope is that we can provide an excellent learning experience to an extremely wide range of interests, and to accomplish that I propose the grading system outlined on the attached sheet. The intention is to provide sufficient flexibility for each student to customize the course to suit individual interests and abilities.

Since I hope this course will be different things for different people, it is difficult to provide a true synopsis here. What should be true for everyone is that this course will give a sort of case study in how, when you examine something closely, mathematical structures emerge on various levels; when you further study those structures, you can learn things that were completely obscure at the initial examination, and in the end you can end up learning deep lessons with applicability far beyond the original field.

Above all else, though, games are fun and this class should be too. I hope you will keep me posted on our progress toward that goal, so we can adjust as needed.

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## Tentative Schedule

|  | Wednesday, January $14^{\text {th }}$ §1.1-§1.3 Basic Techniques | Friday, January $16^{\text {th }}$ <br> §1.4-§1.6 Basic Techniques (cont.) |
| :---: | :---: | :---: |
| Monday, January $19^{\text {th }}$ <br> No Class - MLK Day | Wednesday, January $21^{\text {st }}$ <br> §2.1Game Positions and Options | Friday, January $23^{\text {rd }}$ §2.2 Impartial Games |
| Monday, January $26^{\text {th }}$ <br> §2.3 Case Study: Partizan Endnim | Wednesday, January $28^{\text {th }}$ §3.1 Sums of Games | Friday, January $30^{\text {th }}$ <br> §3.2 Comparisons |
| Monday, February $2^{\text {nd }}$ §3.3 Equality and Identity | Wednesday, February $4^{\text {th }}$ §3.4 Case Study: Domineering | Friday, February $6^{\text {th }}$ §4.1 Algebra |
| Monday, February $9^{\text {th }}$ <br> §4.1 Algebra (cont.) | Wednesday, February $11^{\text {th }}$ §4.2 Order | Friday, February $13^{\text {th }}$ <br> §4.2 Order (cont.) |
| Monday, February $16^{\text {th }}$ §4.3 Canonical Form | Wednesday, February $18^{\text {th }}$ §4.3 Canonical Form (cont.) | Friday, February $20^{\text {th }}$ 4.4 Incentives |
| Monday, February $23^{\text {rd }}$ <br> 4.4 Incentives (cont.) | Wednesday, February $25^{\text {th }}$ §5.1 Numbers | Friday, February $27^{\text {th }}$ <br> §5.1 Numbers (cont.) |
| Monday, March $2^{\text {nd }}$ Classical Game Theory I | Wednesday, March $4^{\text {th }}$ Classical Game Theory II | Friday, March $5^{\text {th }}$ Classical Game Theory III |
| Spring Break |  |  |
| Monday, March $16^{\text {th }}$ §5.2 Up, Down, and Star | Wednesday, March $18^{\text {th }}$ §5.3 Switches | Friday, March $20^{\text {th }}$ §6.1 Games Born by Day 2 |
| Monday, March $23^{\text {rd }}$ §6.2 Games Born by Day $n$ | Wednesday, March $25^{\text {th }}$ §6.2 Games Born by Day $n$ | Friday, March $27^{\text {th }}$ §6.3 Stops |
| $\begin{gathered} \text { Monday, March } 30^{\text {th }} \\ \text { §6.3 Stops } \end{gathered}$ | Wednesday, April ${ }^{\text {st }}$ §6.4 More about Numbers | Friday, March $3^{\text {rd }}$ <br> §6.4 More about Numbers (cont.) |
| Monday, April $6^{\text {th }}$ <br> §7.1 Stars Revisited | Wednesday, April $8^{\text {th }}$ <br> Student Research Symposium | Friday, April $10^{\text {th }}$ <br> §7.2 Analysis of Nim |
| Monday, April $13^{\text {th }}$ §7.3 Adding Stars | Wednesday, April $15^{\text {th }}$ §7.4 A More Succinct Notation | Friday, April $17^{\text {th }}$ <br> §7.5 Taking-and-Breaking Games |
| Monday, April $20^{\text {th }}$ §7.6 Subtraction Games | Wednesday, April $22^{\text {nd }}$ <br> §8.1 Comparing Games and Numbers | Friday, April $24^{\text {th }}$ <br> §8.2 Coping with Confusion |
| Monday, April $27^{\text {th }}$ §8.3 Cooling | Wednesday, April $29^{\text {th }}$ <br> Presentations |  |
| Final Exam - 8am on Friday, May $1^{\text {st }}$ |  |  |

Any students with disabilities which might affect their performance in this class should contact me as soon as possible to arrange accommodations.

Coe's faculty has adopted an academic integrity policy. It is your responsibility to understand and follow it.

Diversity, in all its forms, is valuable.

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## Grading Scheme

Grades will not be point-based, but rather activity-based. Earning a certain grade in this class will require accomplishing a certain number of tasks, rather than performance on selected examinations. The following table specifies the requirements for each grade:

|  | A | $\mathrm{A}-$ | $\mathrm{B}+$ | B | $\mathrm{B}-$ | $\mathrm{C}+$ | C | $\mathrm{C}-$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Participation | $40+$ | $40+$ | $39+$ | $39+$ | $39+$ | $38+$ | $38+$ | $38+$ |
| Games | $60+$ | $55+$ | $50+$ | $45+$ | $40+$ | $35+$ | $30+$ | $25+$ |
| Minor Projects | $9+$ | $8+$ | $7+$ | $6+$ | $5+$ | $4+$ | $3+$ | $2+$ |
| Major Projects | $3+$ | $3+$ | $2+$ | $2+$ | $2+$ | $1+$ | $1+$ | $1+$ |
| Presentations | $2+$ | $2+$ | $1+$ | $1+$ | $1+$ | $1+$ | $1+$ | $1+$ |
| Math Culture | $12+$ | $11+$ | $10+$ | $9+$ | $8+$ | $7+$ | $6+$ | $5+$ |
| Quests (Superior) | $90 \%+$ | $85 \%+$ | $80 \%+$ | $75 \%+$ | $70 \%+$ | $60 \%+$ | $55 \%+$ | $50 \%+$ |
| Quests (Acceptable) | $100 \%+$ | $100 \%+$ | $95 \%+$ | $95 \%+$ | $95 \%+$ | $90 \%+$ | $90 \%+$ | $90 \%+$ |

The "Games" category represents games you try playing during the semester which you have never played previously. At least $50 \%$ of these must be combinatorial games. At least 15 minutes of play is required, along with brief documentation in a Game Journal where you record your impression of the game, immediate conjectures, ideas about strategies, relations to other games, and other related notes. Students should select games to represent a wide variety, without excessive representation of any one category.
"Minor Projects" are expected to constitute 2-4 hours of effort and "Major Projects" 5-9 hours. All projects should be planned in consultation with the instructor, and in many cases group efforts will be appropriate. At least two projects must include a significant written portion, with revision encouraged.
"Quests" will be evaluations somewhere between quizzes and tests, generally undertaken on an individual basis. The table lists what share must be submitted at a superior level, and what share can be at just an acceptable level, for each grade.

At least one third (rounded judiciously) of the required quota in each category must be completed by midterm (March 6 ${ }^{\text {th }}$ ). For this purpose, "Major Projects" and "Presentations" will be considered a single category.

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## Math Culture Points

A significant portion of the grade for this course will take the form of Math Culture Points. These will be earned through activities outside of class including, but not necessarily limited to, those listed below:

| Activity | Points | Max \# |
| :---: | :---: | :---: |
| Colloquium Attendance | 1 | - |
| Colloquium Presentation | 1-3 | 2 |
| Meeting Attendance <br> Midwest Undergraduate Mathematics Symposium (April $3^{\text {rd }}-4^{\text {th }}$ ) <br> Nebraska Conference for Undergraduate Women in Mathematics (Jan. 30 ${ }^{\text {th }}-$ Feb. $1^{\text {st }}$ ) | 3 | 2 |
| Mathematics Competition Participation <br> Iowa Collegiate Mathematics Competition (Feb. $28^{\text {th }}$ ) Mathematical Contest in Modeling (Feb. $5^{\text {th }}-9^{\text {th }}$ ) | 2 | 2 |
| Math Culture Reading <br> Some weeks specific readings will be posted on the course web page With approval, any column on MAA.org With approval, an article from Math Horizons, CMJ, etc. | 1 | $\begin{gathered} - \\ 5 \\ 5 \end{gathered}$ |
| Math Club Activities (when appropriate) <br> Winter Break Book, Movies, Pi Day celebration, Speakers, etc. | 1 | 5 |
| Volunteer Math Outreach <br> Working with students at Polk Elementary, etc. | 1 | 3 |
| Other Appropriate Coe Activities <br> Attending a Quantitative Research Symposium Presentation Poverty Simulation <br> Psychology Experiment Participation <br> Contemporary Issues Forum | 1 | $2$ |

Generally Math Culture Points can be earned for at most two activities in any given week, so you should plan to spread your participation throughout the semester. In each case above, credit assumes both full participation and posting a brief summary/response on Moodle. These reflections should generally be between 100 and 300 words, and include both a brief summary and your personal thoughts on the event, and must be submitted within one week of the event.

