## Exam 3a Calc 2 4/1/2011

Each problem is worth 10 points. For full credit provide complete justification for your answers.

1. a) Write the first three terms in the sequence $\left\{\frac{n}{n+2}\right\}$.
b) Write the first three partial sums of the series $\sum_{n=1}^{\infty} \frac{n}{n+2}$.
2. Find the sum of the series $\frac{3}{4}-\frac{1}{2}+\frac{1}{3}-\frac{2}{9}+\frac{4}{27}-\ldots$.
3. Set up an integral for the area inside one loop of the curve $r=\sin 2 \theta$.

4. Find a general solution to the differential equation $\frac{d \Gamma}{d}=(2)(1)-$
5. Find an equation for the ellipse with vertices at $(0,0),(4,0),(2,3)$, and $(2,-3)$.
6. A cup of coffee starts at $200^{\circ} \mathrm{F}$ and cools according to the differential equation $\frac{d T}{d t}=0.05(70-T)$. Using $\Delta t=5$ minutes, approximate the temperature of the coffee after 10 minutes.
7. Biff is a Calculus student at Enormous State University, and he's having some trouble. Biff says "Crap. There was this question on our test about the area of a circle if you do it in polar, right? And it was like $r=2 \cos \theta$, which I graphed it and it gets a circle with the radius is one, right? But so I did it on my calculator and got the area to be $2 \pi$, which I'm pretty sure is wrong. I mean, about the only thing I learned in high school was that the area of a circle is $\pi r^{2}$, and now that's screwed up too!"

Explain clearly to Biff what likely went wrong with his calculation.
8. Find the slopes of the lines tangent to the curve with parametric equations

$$
\mathrm{x}(t)=\cos 3 t \quad y(t)=2 \sin t
$$

at the points where the curve crosses itself.

9. An ellipse can be expressed by the parametric equations

$$
x(t)=a \cos t \quad y(t)=b \sin t .
$$

Use this parametrization to find the area of the ellipse.
10. Set up an integral for the length of the cardioid $r=1+\sin \theta$.

Extra Credit (5 points possible):
Evaluate the integral you set up in \#10 [Hint: One option is to multiply top and bottom by $\sqrt{2-2 \sin \theta}]$.

