



3. A force of 5 pounds is required to hold a spring stretched 0.4 feet beyond its natural length. How much work (in foot-pounds) is done in stretching the spring from its natural length to 0.7 feet beyond its natural length?

4. The region bounded between  $y = 1/x$ ,  $y = 2$ ,  $x = 1$ , and  $x = 5$  is rotated around the  $x$ -axis. Set up an integral for the volume of the resulting solid.

5. Find a solution to the differential equation  $\frac{dy}{dx} = \frac{x}{y}$  that satisfies the initial condition  $y(0) = -3$ .

6. Find  $\bar{x}$ , the  $x$ -coordinate of the centroid of the first-quadrant portion of a circle with radius 1 centered at the origin.

7. Bunny is a Calculus student at Enormous State University, and she's having some trouble. Bunny says "Ohmygod, Calc is so impossible! It's totally unfair! And my teacher has such an accent! Like, there's the disco method and the washo method, I guess? And they're kinda alike but they're not? I'm so confused!"

Help Bunny out by explaining similarities and differences between the disc and washer methods.

8. An aquarium 3m long, 2m wide, and 1.5 m deep is full of water. Set up an integral for the amount of work required to pump all of the water in the tank up to a height 1 m above the top of the tank.

9. [Stewart] A hawk flying 15 m/s at an altitude of 180 m accidentally drops its prey. The parabolic trajectory of the falling prey is described by the equation

$$y = 180 - \frac{x^2}{45}$$

until it hits the ground. Set up an integral for the distance traveled by the prey from the time it's dropped until it hits the ground.

10. The solid formed by rotating the curve

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

where  $a > b$ , about the  $y$ -axis is called an oblate spheroid, and is essentially the shape of most planets (including Earth). Find the surface area of this solid.

Extra Credit [5 points possible]: Think about what happens when you add up numbers of the form  $\frac{1}{n(n+1)}$ , for integer values of  $n$  that start with 1 and continue upward to some value  $k$ . What can you say about the result?