

Four of these problems will be graded (our choice, not yours!), with each problem worth 5 points. Clear and complete justification is required for full credit. You are welcome to discuss these problems with anyone and everyone, but you must write up your own final submission without reference to any sources other than the textbook and instructor.

1. Do the Chapter 1 Followup assignment on WeBWorK, available via

<https://webwork.coe.edu/webwork2/MTH-215/>

2. Consider the formula $1 + 2 + 3 + \dots + n = \frac{n^2+n+1}{2}$.

- (a) Write the formula in sigma notation.
- (b) Show that if this formula works for $n = k$, then it also must work for $n = k + 1$.
- (c) Explain why mathematical induction does not prove that this formula is true for all $n \in \mathbb{N}$.

3. For any $n \in \mathbb{Z}^+$,

$$\sum_{i=1}^n (2i - 1) = n^2$$

4. Prove that if A has n elements, then $\mathcal{P}(A)$ has 2^n elements. [Hint: Induction!]
5. For any sets A and B , $(A \cap B)' = A' \cup B'$.
6. If $A \subseteq B$ and $C \subseteq D$, then $A \cap C \subseteq B \cap D$.
7. Show that $A - (B \cap A) = (A - B) \cap A$.

8. Show that

$$\left(\bigcup_{i \in I} A_i \right)' = \bigcap_{i \in I} A_i'$$

9. Show that

$$A \cup \bigcap_{i \in I} B_i = \bigcap_{i \in I} (A \cup B_i)$$