

Each problem is worth 5 points. Clear and complete justification is required for full credit.

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|--------|---|---|---|---|---|---|
| x | 1 | 2 | 3 | 4 | 5 | 6 |
| $f(x)$ | 4 | 6 | 1 | 2 | 3 | 5 |
| $g(x)$ | 2 | 4 | 6 | 3 | 1 | 5 |

1. Use the table above to evaluate

$$a) f \circ g(2) = f(g(2)) = f(4) = 2$$

$$b) g \circ f(2) = g(f(2)) = g(6) = 5$$

2. Find an exponential function for the form $f(x) = C a^x$ passing through the points (0,3) and (2,12).

Since it goes through (0,3):

$$(3) = C \cdot a^{(0)}$$

$$\therefore C = 3$$

Since it goes through (2,12):

$$(12) = 3 \cdot a^{(2)}$$

$$4 = a^2$$

$$\therefore a = 2$$

$$f(x) = 3 \cdot 2^x$$

3. Evaluate $\log_2 \frac{1}{4}$ exactly.

$$\log_2 \frac{1}{4} = \underbrace{\log_2}_{\text{means}} 2^{-2} = \textcircled{-2}$$

means "What's the exponent you'd put on 2 to get..."

4. Evaluate $\ln \sqrt{e}$ exactly.

$$\ln \sqrt{e} = \underbrace{\log_e}_{\text{means}} e^{\frac{1}{2}} = \textcircled{\frac{1}{2}}$$

means "What's the exponent you'd put on e to get..."